Cut a hole large enough to fit the top of the container through. Then cut a smaller section to the side that tightly fits the body of the cup, below the rim. The cup lifts up through the larger hole and slides into the smaller space. Drill holes to fit your regular selection of brushes.

Big enough for handles to fit,

small enough so the heads don't slip through.